

# SEARUMS: Studying Epidemiology of Avian Influenza Rapidly Using Modeling and Simulation

Dhananjai M. Rao\*, Alexander Chernyakhovsky† and Victoria Rao‡

*Abstract*—Effectively combating avian influenza using constrained resources requires strategic planning and preemptive deployment of countermeasures. However, success of such proactive approaches is contingent on accurate and rapid forecasting of epicenters and time lines of outbreaks using epidemiological analyses. A pragmatic and effective methodology for such epidemiological analysis is computer-based simulation. However, effectively using simulations requires a sophisticated, efficient, and user-friendly software environment for modeling, simulation, and analysis. Accordingly, we have developed an user-friendly, extensible, and portable software environment called SEARUMS in Java. SEARUMS enables modeling, simulation, and epidemiological analysis of avian influenza including prediction of time lines, epicenters, and economic impacts of disease outbreaks. The analysis is performed using a composable, individual agent-based, spatially explicit model seeded with real world statistical data. Simulations are performed using a high performance, multi-threaded discrete event kernel built into SEARUMS. This paper presents the design and implementation of SEARUMS. The design rationale and implementation issues are discussed along with some of the lessons learned. The paper also presents experiments conducted to validate SEARUMS and verify its scalability.

*Keywords:* Avian Influenza, Spatially explicit model, Agent-based model, Discrete Event Simulation.

## 1 Introduction and Motivation

Avian influenza commonly refers to the disease caused by H5N1, a highly virulent strain of the influenza-A virus [4, 15]. It is known that the virus has become endemic to waterfowl in certain areas and it readily transmits within the Anatidae family, primarily through contaminated feed and feces [4, 11]. In spring 2006, it has been established that migrating waterfowl are the primary vectors responsible for intercontinental spread of the disease [10, 11]. The H5N1 virus readily transmits from infected waterfowl to poultry causing 100% mortality with incubation periods shorter than 48 hours [16]. Avian influenza has caused significant economic hardships at a global scale in the past few years [3]. Moreover, the pathogen also spreads to humans through direct contact with infected poultry and contaminated surfaces causing human fatalities [16]. Therefore,

avian influenza is considered one of the most ominous threat to World economy and mankind.

Accordingly, significant effort and investments are being expended to combat the disease by various international organizations and government agencies, including the World Health Organization (WHO) [15], Food and Agriculture Organization (FAO), and the Centers for Disease Control and Prevention (CDC) [4]. Currently, strategic deployment of vaccinations is the primary mechanism for prevention of avian influenza [4, 16]. Unfortunately, a myriad of technological and socio-political issues have rendered manufacturing and distribution of H5N1 vaccine a significant challenge [4, 16]. Consequently, the only realistic approach to combat the disease is through proactive planning and strategic deployment of countermeasures [4, 16]. However, the success of such proactive approaches is contingent on availability and accuracy of forecasts on epicenters and time lines of disease outbreaks.

Forecasting disease outbreaks requires comprehensive analysis of the disease's epidemiology which is characterized by global, symbiotic interactions between the three main entities, namely: migrating waterfowl [5, 10, 11], poultry, and humans [3]. Analyzing the epidemiology is a significant challenge due to its stochastic time dependent nature, large size, complexity, and nascence. The only realistic methodology to rapidly analyze such a complex, stochastic system is computer-based simulation. Simulation is widely employed for study and analysis of complex systems because it is a straightforward, cost effective, and non-destructive methodology for the study and analysis of a wide spectrum of systems. It enables explorations of complicated scenarios that would otherwise be difficult or impossible to analyze.

Needless to emphasize, realizing the advantages of simulation-based methodologies requires the use of an effective software environment for modeling, simulation, and analysis [12]. Specifically, in this case, the software environment must be conducive for analyzing the epidemiology of avian influenza. It is imperative for the software system to be intuitive and robust to enable its use by domain experts who may not be adept programmers [12]. Moreover, the software must be portable and accessible to enable collaborative use. Currently, there is no M&S environment that is geared to ease study and analysis of epidemiology of avian influenza while satisfying the aforementioned criteria. Consequently, we have endeavored to design and develop such a software

\*CSA Department, Miami University, Oxford, OH 45056. USA. Email: raodm@muohio.edu

†Mason High School, Mason, OH 45040. USA.

‡Cybernetic Evolution, Inc., Mason, OH 45040. USA. Email: victoria@CyberneticEvolution.com

environment called SEARUMS.

SEARUMS is an acronym for Studying Epidemiology of Avian Influenza Rapidly Using Modeling and Simulation. It is a Java-based integrated, graphical modeling, simulation, and analysis environment that is specialized for epidemiological study of avian influenza. It provides an extensible, agent-based, spatially explicit modeling front-end coupled with a discrete event simulation kernel and libraries for plotting graphs and charts for analysis. In addition, SEARUMS also includes comprehensive models that incorporate real-world statistical data on: waterfowl migration, published by Global Register Of Migratory Species (GROMS) [6]; waterfowl species that are at higher risk to carry the virus [3]; global poultry population and distribution, published by the Food and Agriculture Organization (FAO) of the United Nations [1]; and human population in metropolitan areas of the United States, obtained from the U.S. Census Bureau. The model is stored as a portable XML document that can be readily reused and further extended.

This paper describes the design and implementation of SEARUMS. Section 2 presents some of the software environments that were explored as a part of this research. These software environments also represent closely related research activities. The architecture of SEARUMS is discussed in Section 3 along with selected implementation details. Verification of the models developed using SEARUMS is discussed in Section 4 along with performance experiments. Section 5 concludes the paper, discussing some of the lessons learned along with pointers to future work.

## 2 Related Research

SEARUMS leverages individual, Agent-based Spatially Explicit (ASE) modeling methodology and Discrete Event Simulation (DES) technique to enable epidemiological analysis of avian influenza. Impetus for such a Modeling and Simulation (M&S) approach, involving ASE models and DES, stems from its advantages [9, 12, 13] and popularity [9, 12]. Several ecological M&S environments and frameworks that utilize such an approach have been reported. Some of the related M&S software, that are similar to SEARUMS, are briefly described in this section. Furthermore, they are also compared and contrasted with SEARUMS to elucidate some of the factors motivating the design and implementation of SEARUMS.

Railsback *et al* have reviewed five popular, general purpose software platforms for scientific, agent-based M&S [12]. The platforms include NetLogo, Swarm, Swarm Java, Repast, and MASON. In their review, NetLogo was highly recommended for its ease-of-use. However, it uses a custom language for modeling and its source code is proprietary. Therefore, it poses interoperability issues. On the other hand, the latter four platforms uses traditional programming languages and source codes are freely available. These four platforms essentially provide a core framework for model development and a collection of library modules. The library modules are built using

the core framework and can be readily reused for modeling. SWARM, written in Objective-C, is reported to be one of the most mature environments [12]. However, Objective-C is not widely used, is not native to all platforms, and lacks developer tools [12]. SWARM Java provides a Java interface to Swarm's Objective-C libraries to improve portability and interoperability. Nevertheless, Railsback *et al* report that Java Swarm does not combine the advantages of the two languages well. Furthermore, SWARM was reported to have lower performance for larger models [12]. Hence SWARM and SWARM Java were not viable candidates for developing SEARUMS, that we envision to be fast, portable, and interoperable. On the other hand, Repast and MASON are pure Java-based environments with slightly different design objectives. The focus of Repast is primarily on the domain of social science and includes tools specific to that domain [12]. MASON has been designed as a smaller and faster alternative to Repast with focus on computationally demanding models. Although MASON is the fastest simulator amongst these software environments, it is the least mature and requires additional libraries for compilation. Consequently, the design of SEARUMS was steered away from Repast and MASON.

The High Level Architecture (HLA) and a web-enabled parallel simulation environment called WESE [13] were also explored as potential candidates for developing simulations. HLA was disregarded because it requires a commercial Runtime Infrastructure (RTI) software and a federate library that can be cost prohibitive. WESE was not a viable alternative because it has been designed for batch simulations and does not provide an effective mechanism to interface with a GUI. The aforementioned drawbacks of various software systems motivated us to custom develop SEARUMS. The design and implementation of SEARUMS as discussed in the next section.

## 3 SEARUMS

SEARUMS is an acronym for Studying Epidemiology of Avian influenza Rapidly Using Modeling and Simulation. It has been developed in Java by capitalizing on many of its object oriented programming features [2]. SEARUMS is designed to be an user friendly, integrated, graphical modeling, simulation, visualization, and analysis environment for conducting epidemiological analysis of avian influenza using an Agent-based, Spatially Explicit (ASE) model. These design goals have been achieved by composing the system using a collection of interdependent but loosely coupled modules. Each module has a well defined functionality that can be accessed and utilized via a set of Application Program Interface (API) method calls. The API of modules are essentially Java interface classes that are implemented by each module. Interactions between modules are performed via interface classes to ensure loose coupling. This approach permits seamless plug-n-play of modules and the environment is composed by loading suitable modules dynamically on-demand via Java's reflection API [2]. Such an implementation approach has been

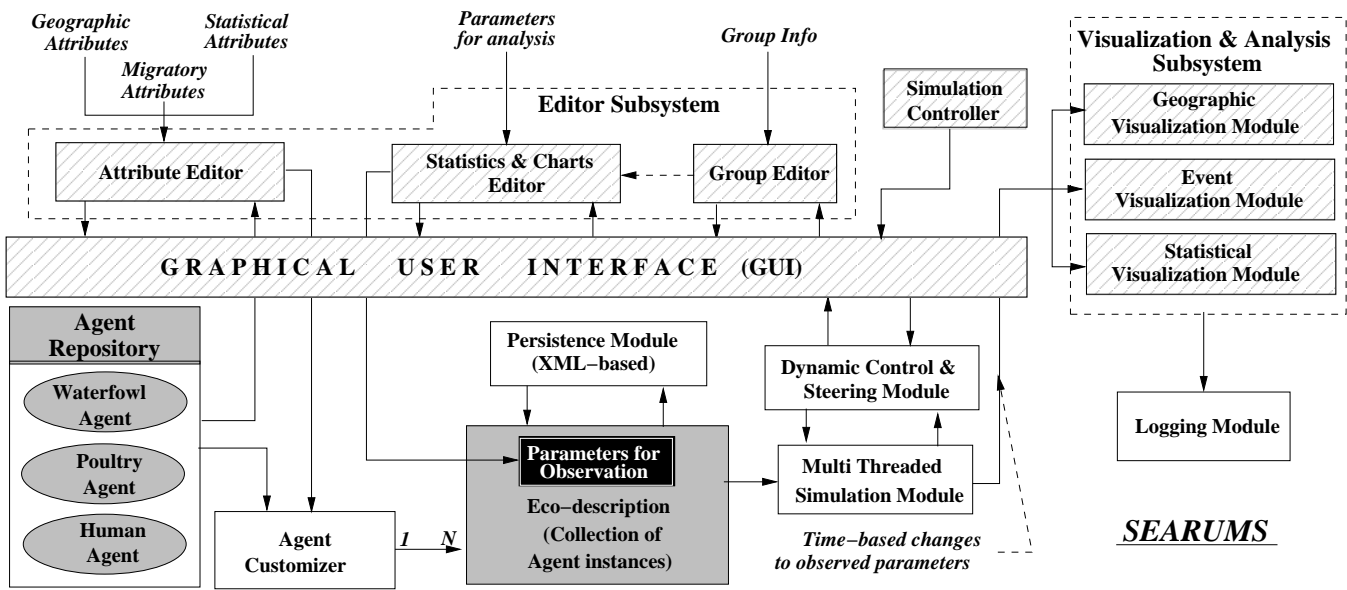


Figure 1: Architectural overview of SEARUMS. GUI modules are highlighted with a striped background. SEARUMS can be downloaded from <http://www.searums.org>.

adopted to ease customization and extension of SEARUMS without requiring changes to its design or impacting existing modules.

An architectural overview of the modules constituting SEARUMS is shown in Figure 1. The modules can be broadly classified as core modules and Graphical User Interface (GUI) modules. The core modules of SEARUMS are Agent Repository, Agent Customizer, Persistence Module, Dynamic Control & Steering Module, Simulation Module, and Logging Module. These modules provide the core M&S functionality of SEARUMS. The GUI facilitates interactions with the core modules via convenient and intuitive user interfaces. The GUI modules can be further categorized into the Editor subsystem, the Simulation Controller, and the Visualization & Analysis subsystem. SEARUMS uses the Model-View-Controller pattern to couple the core modules, the GUI models, and the Eco-description. The design permits the GUI modules to be easily replaced with a minimal command-line text interface for running SEARUMS in offline batch mode. The batch mode is useful for performing repeated runs or analyzing different scenarios on computational clusters.

The modules and subsystems constituting SEARUMS cooperatively operate on a shared, in-memory representation of the model called the Eco-description. The Eco-description is a centralized, in-memory data structure that includes all the information necessary for modeling, simulation, and analysis. It is composed using a collection of Java classes and that provide efficient access to data and information required by the various modules. The primary information encapsulated by the Eco-description relates to the smart agents [8] that constitute the model. As shown in Figure 1, the agents are organized into an Agent Repository to facilitate instantiation and use via Java reflection API. Currently, SEARUMS includes

the following three smart agents: Waterfowl Agent that represents a migrating waterfowl flock, Poultry Agent that models behavior of poultry flocks, and Human Agent that models humans. Each agent has its own behavior that reflects the characteristics of its real-world counterpart. The behaviors are customized to represent specific instances of an agent by specifying suitable values for the exposed attributes via the Attribute Editor GUI module. The attributes of an agent include:

1. *Geographic attributes* that indicate the location (latitude and longitude) and logical association with countries and continents. In addition, each agent has a circle or influence that circumscribes its neighborhood.
2. *Migratory attributes* are specified only for agents whose location changes over the lifetime of the simulation. The migratory attributes are described as a sequence of migration points. Each migration point has geographical and chronological (arrival and departure dates) attributes associated with it. In SEARUMS, only one complete migration cycle needs to be specified. The software automatically reuses the information to simulate annual migratory cycles.
3. *Statistical attributes* for agent instances include their initial population, density and distribution, initial infection percentage, infection spread parameters, incubation periods, mortality rates, and population regrowth parameters.

The agents essentially implement the conceptual, mathematical model of the system developed using Markov processes. They are added to a model via suitable toolbar buttons or menu options provided by SEARUMS. Agent instances are created with default attributes from the Agent Repository by the Agent Customizer module using Java's reflection API. Once instantiated, the attributes for agents can be modified

via the Attribute Editor module. The agents are implemented as a family of Java classes by extending a common base class called `Agent`. The `Agent` class provides methods for interacting with the simulation kernel, inspecting the neighborhood, scheduling events, and interfacing with the GUI modules.

The agents in a model are logically organized into hierarchical sets called groups. SEARUMS permits multiple top-level groups with an arbitrary number of hierarchies, with one or more sub-groups at each hierarchical level. An agent can be a member of multiple groups. The groups serve several different purposes in SEARUMS. A group can be used as a parameter for statistical analysis and for plotting charts. For example, a group called “United States” can be created with 50 different sub-groups, one for each state, encompassing various agents. The main “United States” group can be selected for plotting charts and SEARUMS automatically collates and plots data for each state. Note that, even though graph plotting is restricted to one hierarchical level, statistics for plotting are collated in a recursive, depth-first manner and includes data from all agents in underlying hierarchies. A modeler can use a combination of groups to perform multi-faceted analysis at different scales. In addition, groups can be included or excluded from simulations for analyzing different scenarios. The GUI modules utilize groups to provide control on visibility of agents to manage details displayed on the screen. The Group Editor module provides the user interface for managing group entries and hierarchies.

Once all the agent instances and groups have been established in a model, the parameters for observation are added to the Eco-description. These parameters are selected by the user via the Statistics & Charts Editor from a list of options. The list includes the attributes of the agents and the groups in the Eco-description. Each parameter is configured to be sampled hourly, daily, or weekly in terms of simulation time. Moreover, each parameter can be subjected to statistical operations, such as sum, mean, and median. SEARUMS can dynamically (*i.e.*, during simulation) plot and save a variety of charts including: line graphs and pie charts. Multiple charts can be simultaneously used for analyzing a variety of data.

All of the aforementioned information is stored as an integral part of the Eco-description. The Eco-description can be saved for future reuse via the `Persistence Module`. The Eco-description is unmarshalled to an XML document that is compliant with a predefined XML schema. Serializing to an XML document has its advantages. First, it enables simple scripts to be developed that can modify specific values and perform multiple simulation runs in batch mode. Second, XML documents can be readily version controlled and archived using commonly available revision control systems like CVS and Subversion. Third, it eases documentation, validation, sharing, and reuse of valuable domain-specific statistical data collated by different researchers from diverse sources. Such features play an important role in facilitating large-scale, collaborative epidemiological studies.

The Simulation Module performs the task of conducting a Discrete Event Simulation (DES) using the Eco-description. This module utilizes a multi-threaded DES-kernel that manages and schedules the discrete events generated by the Agents. Multi-threading enables the DES-kernel to exploit the compute power of multi-processor or multi-core machines thereby reducing the wall-clock time for simulation. The number of threads spawned by the DES-kernel is configurable. Each thread processes concurrent events (events with the same timestamp) in parallel without violating the causal constraints between events. The Dynamic Control and Steering Module provides the infrastructure to control the DES-kernel. In addition, it permits selected agent attributes to be modified during the course of simulation. The Simulation Controller module provides the graphical interface to the Dynamic Control & Steering Module.

## 4 Experiments

Several experiments have been conducted to evaluate the effectiveness of SEARUMS. The initial experiments involved verification and validation of the simulations conducted using SEARUMS. For this purpose, we have developed an Eco-description using selected, high risk species of waterfowl as reported by Hagemeyer *et al* [7]. Table 1 lists the waterfowl species, including high risk species [7], used in the model. The migratory flyways of the waterfowl and their population has been collated from data published by various organizations [1, 4, 6, 7, 14, 15]. For modeling and simulation purposes the dates for migration were approximated to the middle of the months reported in the statistics. The initial positions of the flocks were set to correspond to 01/01/2006, which is the real-world time when this specific simulation is logically set to commence. The dispersion of poultry population in different continents has been approximated to circular regions with even density in the Eco-description [1, 9]. Poultry data has been collated from statistics published by national organizations and government databases [1]. Currently, we have represented human population, as reported by U.S. Census Bureau [14], only in 26 major metropolitan areas of the United States, approximated to circular regions. However, the Eco-description can be readily extended to include other parts of the world. Note that to the best of our knowledge, it is the most comprehensive model of its kind reported to date.

Having developed the Eco-description, we verified validity of the Eco-description by performing extensive simulations with initial source of infection set to outbreak in Indonesia [16]. We established validity of the Eco-description and SEARUMS by confirming that the timing and chronology of several outbreaks observed in the simulations correlate with significant real-world incidents as reported by WHO [16]. The data in Table 2 presents a comparison of real-world and simulated outbreaks. The data is presented for some of the significant, initial avian influenza outbreaks and not for repeated outbreaks that occur in these regions. Note that deviations of  $\pm 2$  weeks is expected due to approximation of migration dates. In addition,

| Description of Agent Type | No. of Agents | Total Population      | CMP       |
|---------------------------|---------------|-----------------------|-----------|
| Bar-Tailed Godwit         | 4             | 40,000                | 18        |
| Canada Goose              | 16            | 231,700               | 5         |
| Common Crane              | 9             | 225,000               | 21        |
| *Eurasian Widgeon         | 3             | 1,296,000             | 17        |
| Great Knot                | 3             | 231,000               | 8         |
| *Mallard                  | 1             | 5,000                 | 1         |
| Razorbill                 | 1             | 148,000               | 4         |
| *Red-Breasted Goose       | 1             | 44,000                | 4         |
| Red-crowned Crane         | 1             | 15,000                | 4         |
| Siberian Crane            | 3             | 30,000                | 12        |
| Yellow-Billed Duck        | 2             | 20,000                | 8         |
| Total waterfowl flocks    | 44            | 5,355,000             | 40        |
| Total Poultry flocks      | 121           | 12,280,000,000        | 32        |
| Total Human groups        | 26            | 125,000,000           | 1         |
| <b>Total</b>              | <b>191</b>    | <b>12,410,355,000</b> | <b>40</b> |

Table 1: Various agent instances used to develop the Eco-description used for experiments. Entries prefixed with \* indicate high risk waterfowl species [7]. The CMP column indicates the number of countries in the flocks migratory flyway. The bird population represented by a set of agents is shown in the Total Population column.

| Incident               | Real-world Date | Simulated Date | Error (Days) |
|------------------------|-----------------|----------------|--------------|
| Outbreak in Indonesia  | 23-Jan-06       | 1-Jan-06       | 22           |
| Infection in Iraq/Iran | 1-Mar-06        | 25-Mar-06      | 24           |
| Infection in China     | 27-Apr-06       | 2-Apr-06       | -25          |
| Infection in Egypt     | 11-Oct-06       | 14-Sep-06      | -27          |

Table 2: Comparison of chronology of significant Real-world outbreaks with simulated outbreaks

deviations in dates also occur because the Eco-description does not include all types of migratory waterfowl flocks but only the high risk species. However, the sufficiently close concordance between simulated and real-world outbreaks establishes validity and effectiveness of SEARUMS. Moreover, it significantly increases confidence in inferences drawn from the simulation. Currently, a variety of case studies using SEARUMS are already underway to predict and avert a pandemic.

The validated Eco-description was also used to conduct scalability and performance evaluation of SEARUMS. The model was simulated using a varying number of threads on a Sun Netra-T12 SMP workstation with eight 1.2 GHz SPARCv9 processors with 16 gigabytes of RAM running Solaris 9. These simulations were conducted by running SEARUMS in batch mode, without any GUI overhead. The core statistics collated from these experiments are shown in Table 3. The CPU Utilization value indicates the actual amount of computational power utilized by the simulations. The maximum value of CPU utilization is 800 for this workstation. The last column

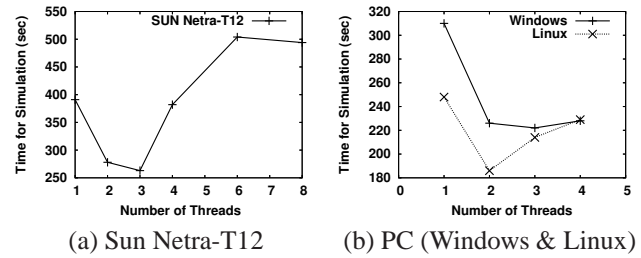


Figure 2: Influence of number of threads on wall-clock time for simulation on different hardware platforms and operating systems.

in Table 3 presents the average number of events processed by each thread in the simulation. The of total number of events in each simulation is 21,045,540. The data in Table 3 indicates that as the number of threads are increased, the threads share the workload involved in processing the events; thereby leveraging the computational capabilities of the workstation.

The graph in Figure 2(a) plots the wall-clock time taken to complete the same simulation using different number of threads. As shown by the curve, initially the time taken for simulation reduces as the number of threads are increased. The wall-clock time decreases because the threads run in parallel on the multi-processor machine and rapidly process concurrent events. The performance improves as the number of threads is increased from one to three highlighting SEARUMS' scalability. However, the performance decreases as the number of threads are further increased. The deterioration occurs because the model used in this experiment does not have sufficient, inherent concurrency to leverage the available compute power. In other words, multi-threading overheads supersede the gains accrued using several threads. The plateauing CPU utilization data shown in the third column of Table 3 confirm that this specific simulation does not require more than three CPUs. On the other hand, larger models with more concurrency will benefit from the scalable design. This experiment highlights the scalability and performance aspects of SEARUMS design. In addition it illustrates its potential use in high performance computational workstations for conducting large-scale epidemiological analysis.

| #Threads | Time (Secs) | CPU Usage |
|----------|-------------|-----------|
| 1        | 391         | 101.5     |
| 2        | 278         | 192.1     |
| 3        | 263         | 267.9     |
| 4        | 382         | 287.7     |
| 6        | 504         | 267.6     |
| 8        | 494         | 278.5     |

Table 3: Scalability and performance statistics collated from simulations conducted on a Sun Netra-T12.

| #Threads | Time (Secs) |       | CPU Usage |       |
|----------|-------------|-------|-----------|-------|
|          | Windows     | Linux | Windows   | Linux |
| 1        | 310         | 248   | -         | 100   |
| 2        | 199         | 186   | -         | 177   |
| 3        | 222         | 214   | -         | 142   |
| 4        | 228         | 229   | -         | 138   |

Table 4: Simulation statistics collated on a PC running Linux or Windows. The CPU usage under Windows is not available. The maximum possible CPU usage is 200, 100 per core.

The aforementioned Eco-description was also used to conduct performance test simulations on a conventional personal computer (PC). The PC had a dual-core, 64-bit Turion processor running at 2 GHz with 2 GB of memory. The PC was setup to a dual-boot configuration enabling it to run Windows XP (32-bit) or Linux (Fedora Core 7). Table 4 tabulates the various statistics collated from simulations conducted using a varying number of threads. Note that the hardware configuration was the same but different operating systems were used. As illustrated by Table 4, the statistics under the two operating systems closely match with each other. The data indicates that SEARUMS operates consistently on the commonly used platforms. The graph in Figure 2(b) plots the wall-clock time for simulation. The performance curves mirror the graph in Figure 2(b). Similarity, in the characteristics further highlights the scalability and portability of SEARUMS from high performance workstations to conventional PCs. Simulations involving more than 20 million events complete within 4 minutes in optimal configurations demonstrating that SEARUMS enables rapid epidemiological analysis of avian influenza. Furthermore, the experiments provide empirical evidence that the design goals of SEARUMS have been successfully achieved.

## 5 Conclusion

This paper discussed the issues involved in the design and implementation of a Java-based modeling, simulation, and analysis environment called SEARUMS. SEARUMS has been designed to facilitate epidemiological analysis of avian influenza. It permits an agent-based, spatially explicit model of avian influenza to be developed using an intuitive Graphical User Interface (GUI). SEARUMS does not require any special computing infrastructure or programming knowledge. The verification experiments presented in this paper highlight that the models developed using SEARUMS closely reflect real world scenario. The simulation provides accurate time lines and locations of outbreaks. Such information is invaluable to epidemiologists and disease control centers. In addition, SEARUMS also provides an offline batch mode for conducting large-scale analysis using high performance computational workstations to analyze various scenarios. Ability to rapidly analyze various scenarios using calibrated models empowers researchers, epidemiologists, and disease control centers with timely information on outbreaks. The Eco-description developed using SEARUMS embodies a broad range of informa-

tion and statistics which by itself is valuable. In addition, the Eco-description can be readily extended, shared, and reused. Consequently, experts from multiple domains can collaboratively use SEARUMS to perform various types of analysis on a global scale, assess threats, and measure effectiveness of countermeasures. We are optimistic that the proposed software environment will enable mankind to strategically invest precious time and resources to combat Avian influenza, minimize its impacts on human life and global economy thereby averting a pandemic.

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